

# Manifesto degli Studi del Corso di Laurea Magistrale in Matematica a.a. 2023-2024

Approvato dal Consiglio di Dipartimento il 19 aprile 2023

#### 1. Activation

The <u>Department of Mathematics</u> promotes the Master of Science in Mathematics (<u>Corso di Laurea Magistrale in Matematica</u>), belonging to the class "LM-40 - Matematica". The Master of Science in Mathematics is aimed at providing an in-depth knowledge and understanding of several areas of advanced Mathematics, and of its relations to other Sciences. Courses of the Master of Science in Mathematics are taught in English.

#### 2. Curricula

The Master of Science in Mathematics is organized into four *curricula*:

- Advanced Mathematics
- Cryptography
- Mathematics and Statistics for Life and Social Sciences
- Teaching and Scientific Communication

Every student is required to formally choose one of the curricula and to follow the corresponding rules as stated in the <u>Regolamento Didattico della Laurea Magistrale in Matematica</u>. Advisors of studies are available for the various curricula. Any change of curriculum is subjected to a verification of the Teaching Committee.

#### 3. Admission requirements

To apply to the Master of Science in Mathematics, a student shall fulfill both some formal requirements and a satisfactory personal qualification.

The following information is required and shall be provided according to the instructions given in the web site:

- to which curricula the applicant is interested in;
- a detailed study plan of the bachelor's degree, including titles and syllabi of all the courses taken;
- a document from the University that issued the bachelor's degree with reporting, in Italian or English, the list of courses, the mark obtained in each of them and the final mark associated with the degree;
- work and professional experiences;
- level of knowledge of English Language, certified by internationally recognized organizations or by the University that issued the bachelor's degree;
- a motivation statement, explaining why the student is willing to apply to the Master of Science in Mathematics, and what he expects from it.

As far as the formal requirements are concerned, a bachelor's degree lasting for three years or longer is mandatory; such a degree must provide a good basic mathematical knowledge, including at least linear algebra, mathematical analysis and some of their applications. A certificate for a B1 level of English is also required.

These formal requirements are satisfied by students who possess a bachelor's degree belonging to the class "L-35 – Scienze matematiche" or a bachelor's degree with at least 60 credits in sectors MAT/XX (credits in sectors FIS/, SECS-S/, INF/01 may also be considered, for courses with a strong mathematical content).

Knowledge and skills of the applicant are evaluated by the Admission Committee of the Department of Mathematics. The evaluation may require a written examination and/or an interview.

The details on the admission procedure can be found as an attachment to this document or <u>on the web site</u>. The student is admitted to one or more chosen curricula or to a different one as decided by the Admission Committee. Some students might be required to follow a particular study plan.

#### 4. Study plan

Students have to submit a study plan, which satisfies the requisites of the chosen curriculum as described in the Regolamento Didattico. A proper study plan must contain at least 120 credits, chosen in the following categories: **core** courses (caratterizzanti), **complementary** courses (affini), **free choice** courses (liberi), **language** courses and Stage/Thesis.

In this document we propose, for each curriculum, specific study plans (called *tracks*) which are suggested to the students; such study plans are approved by default. Students have the opportunity to write a personal study plan within each curriculum: such study plan must comply with the rules contained in the Regolamento Didattico and is subject to approval by the Teaching Committee. Students are not allowed to repeat activities already taken in their earlier career. By the agreement with the University of Verona, students may propose a study plan in which some courses are offered by the Master Degree in Mathematics of that university. By the agreement with SMI (Scuola Matematica Interuniversitaria), students who attended a Summer School and passed the related exam can obtain the recognition of credits, subject to approval by the Teaching Committee.

5. Safety courses The on-line courses "Health and Safety in the workplace General Risk training" (4 hours) and "Health and Safety in the workplace Specific risk training (Low Risk)" (4 hours) are mandatory for all the students attending courses held in computer and/or teaching labs. The courses are available through <u>Didattica online</u>. The course "Health and Safety in the workplace Specific risk training (Low Risk)" is replaced by the course "Safety in the laboratory" for students attending the courses Experimental Physics Laboratory at High School Level I and/or II. The course "Safety in the laboratory" must appear in the study plan (cod. 140551).
Activities provided by other Departments or Stage activities may have other requirements regarding safety courses.

#### 6. Foreign languages

Students are required to get a B2 certificate of English (3CFU). In case the student has already used a B2 certificate of English to get 3CFU in the bachelor's degree, then he/she must obtain 3 CFU with a C1 certificate of English or a B1 certificate of French, German or Spanish or with the course Scientific Writing and Presentations in English. The rules for certificates are the ones fixed by CLA. In particular, the score in every ability should be at least equal to 6/10.

#### **IMPORTANT NOTICE**

#### The curriculum Advanced Mathematics

#### **Prerequisites**

Students are supposed to have a basic knowledge on the following topics and a good comprehension of some of them:

- Algebra (groups and rings, ideals, quotients, isomorphism theorems);
- Geometry (general and algebraic topology, topological and differentiable manifolds, projective geometry);
- Complex Analysis (in one variable);
- Measure Theory (Lebesgue measure and integration theory);
- Ordinary Differential Equations and basic examples of Equations (Laplace, heat and wave equations);
   Functional Analysis (Banach and Hilbert spaces, linear operators);
- Basics of approximation techniques in Numerical Analysis;
- Classical foundations of Mathematical Physics; Probability (axiomatic construction).

The graduates will meet strong demand from the business-oriented environment where problem solving and analytical skills are highly appreciated.

Students are invited to choose between the following options, which are called tracks:

- General Advanced Mathematics
- Advanced Algebra and Geometry
- Calculus of Variations, Partial Differential Equations and Dynamical Systems

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#### Advanced Algebra and Geometry

This track has a strong focus on Algebra, Geometry and their interactions, such as in algebraic geometry. In particular, a firm grasp of core algebraic and geometric notions will be required, such as groups, rings, multivariate polynomials, linear algebra, projective geometry, topological spaces, functions of one complex variable. Students will have the possibility to develop a research thesis on Commutative Algebra, Computational Algebra, Lie Theory, Group Theory, Algebraic Curves, Algebraic Surfaces, Higher Dimensional Algebraic Varieties, Real, Complex and Quaternionic Geometry.

The graduates will meet strong demand from the business-oriented environment where problem solving and analytical skills are highly appreciated. The high specialization of this track is well suited for pursuing PHD studies in Italy or abroad, as well as for applying to international fellowships in Pure and Applied Mathematics.

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#### Calculus of Variations, Partial Differential Equations and Dynamical Systems

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This track has a strong focus on subjects as: Calculus of Variations, Partial Differential Equations (mainly theoretical but also numerical), Ordinary Differential Equations and Dynamical Systems.

Beyond the general prerequisites of the Curriculum in Advanced Mathematics, eligible students should have a firm grasp of core topics in Analysis such as: standard notions of ordinary differential equations (linear systems and nonlinear Cauchy problem), basic notions of Partial Differential Equations (Laplace, heat and wave equations, classification), elements of Real Analysis (Lebesgue measure theory, Lebesgue integration theory, L<sup>p</sup> spaces), first elements of Banach and Hilbert spaces, basic probability theory, basic differential geometry.

The students of this track will have the possibility to develop a research thesis on Calculus of Variations, Analysis in metric spaces, Dynamical Systems, geometrical aspects of Partial Differential Equations, Nonlinear Partial Differential Equations, Optimal Control, Numerical Analysis of Partial Differential Equations. The high specialization of this track is well suited for pursuing PHD studies in Italy or abroad, as well as for applying to international fellowships in Pure and Applied Mathematics.

#### The curriculum Cryptography

#### **Prerequisites**

This curriculum has a strong focus on algebra and its applications to coding theory and cryptography. In particular, a firm grasp of core algebraic notions will be required, such as the notion of groups, rings, multivariate polynomial and the arithmetic of finite fields. The ideal candidate is also expected to have some familiarity with geometry, number theory, and probability.

For the stage-oriented track, also some basic programming notions will be useful, such as conditional statements, loops, and functions, as is a willingness to learn and apply more advanced concepts in unfamiliar programming languages. For the research-oriented track, more advanced algebra will be useful, such as fluency in Galois theory and number theory.

In this highly specialized curriculum, the students will receive an introduction to modern methods in Computational Algebra, with an emphasis on its main real-life applications:

According to their own inclination, the students are free to choose between two options:

- Stage-oriented
- Research-oriented

Stage-oriented			

This track is especially aimed at students who wish to work in the security department of a company. Typically, security departments of banks hire our graduates, but also IT companies and security-focused firms find their study preparation of high interest. Indeed, this *track* complements a solid algebraic background with both applied courses, such as *Algebraic Cryptography*, *Applied Cryptography* or *Coding Theory and Applications*, and practical Computer Science courses, such as Java programming (*Laboratorio di Programmazione*) or *Introduction to Computer and Network Security*.

An internship is available for all students. The internship can be either *external* in a company or *internal* within the Laboratory of Cryptography on a project proposed by a company.

Research-oriented

This track is aimed especially at students interested in mathematics research in Applied Algebra, with focus on Cryptography and Coding Theory, and willing to pursue a PhD in Mathematics on these subjects.

#### The curriculum Mathematics and Statistics for Life and Social Sciences

#### **Prerequisites**

Students are supposed to have a basic knowledge on the following topics and a deep comprehension of some of them:

- General Topology;
- Measure Theory (Lebesgue measure and integration theory);
- Functional Analysis (Banach and Hilbert spaces, linear operators, ordinary differential equations, Fourier series):
- Ordinary and Partial Differential Equations
- Numerical Analysis;
- Probability (including its axiomatic construction);
- Mathematical Statistics.

Some basic programming notions will be useful, as is a willingness to learn and apply different programming languages...

Students are invited to choose between the following options, which are called tracks:

- Mathematics for Data Science
- Modelling, Statistics and Analysis of Biosystems
- Modelling and Simulation for Biomedical Applications
- Modelling, Statistics and Analysis in Mathematical Finance

It is also possible for a student to present a personal study plan that may cover applications of mathematics to different fields such as finance, economics, engineering or others. Such a study plan is subject to approval by the Teaching Committee.

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#### Mathematics for Data Science

This track is especially aimed at students who wish to work in Data Analysis departments. Banks, IT companies, medium and large size firms are very interested in students with this kind of preparation. This track is also interesting for those students that would like to pursue a PhD in Statistics and/or Data Science.

Students will have the opportunity to learn the latest developments in Mathematics for Data Science, advanced tools of Probability, Mathematical Statistics, technical aspects in Machine Learning, Deep Learning and Big Data. The emphasis is in the analysis of high dimensional and complex data sets, with applications in various areas such as environmental, biology, social and economic sciences.

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#### Modelling, Statistics and Analysis of Biosystems

This track provides a widespread preparation at the interface between Biological sciences, Mathematics and Informatics.

Students from this *track* have continued with Ph.D. studies and beyond.

An introduction to modern mathematical methods in areas of biology, ecology, epidemiology, molecular networks is provided.

Companies, in particular from the pharmaceutical sector, are interested in students with these competences in modelling and Statistics.

#### Modelling and Simulation for Biomedical Applications

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This track provides the student with the ideal toolbox to design, implement, and apply mathematical models to problems of biomedical and clinical interest. Students will develop solid skills in mathematical modeling, continuum mechanics, differential equations, numerical analysis, machine learning, and scientific computing. Biomedical applications are manifold, including inverse problems, computational hemodynamics, and cardiac modeling. By design, the track has several interactions with clinical research in hospitals, universities, and research centers. Acquired competencies will provide students with a solid background for a Ph.D. in Applied Mathematics or Biomedical Sciences, as well as to work in the biomedical sector or companies with computational model-based R&D departments.

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### Modelling, Statistics and Analysis in Mathematical Finance

The track "Modelling, Statistics and Analysis in Mathematical Finance" aims at preparing students with a modern education in probabilistic, statistical and computational methods.

The Program is entirely taught in English and will provide students with a solid knowledge in key topics of Applied Mathematics, Probability, Statistics and Mathematical Finance.

The track is completed with stages and internships at financial and insurances companies, as well as international research institutions.

## The curriculum Teaching and Scientific Communication

The goal of this curriculum is to cover the spectrum of knowledge and skills required to undertake mathematical teaching at secondary school's level as well as to communicate mathematics and science to a broad public.

#### **Prerequisites**

Students are supposed to have a basic knowledge on the following topics and a good comprehension of some of them:

- Algebra (groups and rings, ideals, quotients, isomorphism theorems),
- Geometry (general and algebraic topology, topological and differentiable manifolds, basic projective geometry),
- Physics (mechanics, thermodynamics, electromagnetism),
- Measure Theory (Lebesgue measure and integration theory),
- Ordinary Differential Equations,
- Classical Foundations of Mathematical Physics,
- Probability (including the axiomatic construction) and Statistics.

Curriculum Advanced Mathematics, Track General Advanced Mathematics										
Advisor of study: Francesco Serra Cassano										
Code	Course	CFU	Hours	SSD	Sem	Lecturer				
MANDATORY										
Foreign la	anguage (3CFU) – See the introduction, po	oint 6								
CORE CO	DURSES									
At least 2	24 credits in sectors MAT/01-05, of which	h at lea	st 15 in ti	he followi	ng table					
145135	Computational Algebra	6	42	MAT/02	1	Alessandra Bernardi				
145130	Advanced Geometry	9	63	MAT/03	1	Roberto Pignatelli				
145129	Advanced Analysis	9	63	MAT/05	1	Francesco Serra Cassano				
The rema	aining credits in the following table:									
145146	Mathematical Logic	6	42	MAT/01	1	Stefano Baratella				
145394	Coding Theory and Applications	6	48	MAT/02	1	Nadir Murru				
145393	Partial Differential Equations (I modulo) Partial Differential Equations (II modulo)	6 3	42 21	MAT/05	1 1	Alberto Valli Alessandro Carlotto				
At least 1	15 credits in sectors MAT/06-09 from th			<u> </u>		Alessandio Canollo				
145435	Stochastic Processes	9	63	MAT/06	1	Stefano Bonaccorsi				
145908	Mathematical Physics - Differential Geometric Methods	9	63	MAT/07	2	Enrico Pagani				
145907	Mathematical Physics - Quantum relativistic Theories	9	63	MAT/07	2	Valter Moretti				
145152	Numerical Methods for PDEs	6	48	MAT/08	2	Robert Nürnberg				
COMPLEMENTARY COURSES - Credits in Core and Complementary courses must be at least 75										
Complen	nentary courses can be chosen in the fo	ollowing	g table:							
145407	Model Theory (*)	6	42	MAT/01	2	Stefano Baratella				
145156	Set Theory (**)	6	42	MAT/01		N.A.				
145131	Algebraic Geometry I	6	42	MAT/03	1	Edoardo Ballico Alessandro Oneto				
145132	Algebraic Geometry II (**)	6	42	MAT/03		N.A.				
145506	Algebraic Topology (*)	6	42	MAT/03	1	Riccardo Ghiloni				
145566	Real Algebraic Geometry (**)	6	42	MAT/03		N.A.				
145557	Advanced Calculus of Variations (**)	6	42	MAT/05		N.A.				
145507	Advanced Topics in Analysis (*)	6	42	MAT/05	1	Gian Paolo Leonardi				
145434	Fourier Analysis	6	42	MAT/05	2	Marco Bonacini				
145538	Geometric Analysis	9	63	MAT/05	2	Lorenzo Mazzieri				
145258	Geometric Measure Theory	6	42	MAT/05	2	Andrea Marchese				
145259	Mathematical control theory (**)	6	42	MAT/05		N.A.				
146115	Minimal surfaces	6	42	MAT/05	1	Alessandro Carlotto				
145159	Stochastic Differential Equations	6	42	MAT/06	2	Michele Coghi Luciano Tubaro				
146211	Optimal transport	6	42	MAT/05	1	Andrea Pinamonti Andrea Marchese				
146212	Toric Geometry (*)	6	42	MAT/03	2	Luis Eduardo Solá Conde Elisa Postinghel				
146213	Dynamical systems (*)	6	42	MAT/05	1	Fabio Bagagiolo				
FREE CH	OICE COURSES				•					

The choice of free courses shall be consistent with the selected curriculum.

Students may use 3 of these CFU to get a C1 certificate of English, a B1 of French, German or Spanish or for the course Scientific Writing and Presentations in English, or to take an internship, according to the rules of the Regolamento.

#### THESIS

The course of studies is concluded with the discussion of an original thesis providing 30 CFU or with

an internship/placement, which assigns 12 CFU, followed by an original thesis providing 18 CFU. Students who choose to take a 3 CFU internship among the free choice courses have to submit an original thesis worth 30 CFU

	Curriculum Advanced Matl	nematio	cs, <i>Trac</i>	k Advar	nced A	lgebra and Geometry			
Advisors of study: Roberto Pignatelli, Willem Adriaan De Graaf									
Code	Course	CFU	Hours	SSD	Sem	Lecturer			
MANDAT	rory	•	•						
Foreign la	anguage (3CFU) – See the introduction, p	oint 6							
CORE C	OURSES								
145135	Computational Algebra	6	42	MAT/02	1	Alessandra Bernardi			
145130	Advanced Geometry	9	63	MAT/03	1	Roberto Pignatelli			
145129	Advanced Analysis	9	63	MAT/05	1	Francesco Serra Cassano			
145435	Stochastic Processes	9	63	MAT/06	1	Stefano Bonaccorsi			
One cou	rse among the following:								
145908	Mathematical Physics - Differential Geometric Methods	9	63	MAT/07	2	Enrico Pagani			
145907	Mathematical Physics - Quantum relativistic Theories	9	63	MAT/07	2	Valter Moretti			
COMPLE	EMENTARY COURSES								
At least	33 credits chosen in the following table	):							
145407	Model Theory (*)	6	42	MAT/01	2	Stefano Baratella			
145156	Set Theory (**)	6	42	MAT/01		N.A.			
145560	Advanced Group Theory (*)	6	42	MAT/02	1	Mima Stajnokovski			
145953	Advanced Number Theory (**)	6	42	MAT/02		N.A.			
145131	Algebraic Geometry I	6	42	MAT/03	1	Edoardo Ballico Alessandro Oneto			
145132	Algebraic Geometry II (**)	6	42	MAT/03		N.A.			
145506	Algebraic Topology (*)	6	42	MAT/03	1	Riccardo Ghiloni			
145566	Real Algebraic Geometry (**)	6	42	MAT/03		N.A.			
145538	Geometric Analysis	9	63	MAT/05	2	Lorenzo Mazzieri			
146212	Toric Geometry (*)	6	42	MAT/03	2	Luis Eduardo Solá Conde Elisa Postinghel			

Students in this track are highly recommended to choose the free courses among the courses in settori MAT/02-03.

The courses can also be taken from the Bachelor's degree, among the following: *Algebra Commutativa*, *Geometria Differenziale*, *Teoria algebrica dei numeri, Introduzione alla Geometria Algebrica* and *Teoria di Galois*, if the student has not taken a similar course in the Bachelor's degree.

Students may use 3 of these CFU to get a C1 certificate of English or a B1 of French, German or Spanish or for the course Scientific Writing and Presentations in English, or to take an internship, according to the rules of the Regolamento.

#### THESIS

The course of studies is concluded with the discussion of an original thesis providing 30 CFU or with

an internship/placement, which assigns 12 CFU, followed by an original thesis providing 18 CFU. Students who choose to take a 3 CFU internship among the free choice courses have to submit an original thesis worth 30 CFU

# Curriculum Advanced Mathematics, Track Calculus of Variations, Partial Differential Equations and Dynamical Systems

Advisors of study: Gian Paolo Leonardi, Francesco Serra Cassano

Code	Course	CFU	Hours	SSD	Sem	Lecturer			
MANDATORY									
Foreign language (3CFU) – See the introduction, point 6									
CORE COURSES									
145130	Advanced Geometry	9	63	MAT/03	1	Roberto Pignatelli			
145129	Advanced Analysis	9	63	MAT/05	1	Francesco Serra Cassano			
145393	Partial Differential Equations (I modulo) Partial Differential Equations (II modulo)	6 3	42 21	MAT/05	1 1	Alberto Valli Alessandro Carlotto			
145435	Stochastic Processes	9	63	MAT/06	1	Stefano Bonaccorsi			
145152	Numerical Methods for PDEs	6	48	MAT/08	2	Robert Nürnberg			
COMPLEMENTARY COURSES - 36 credits chosen in the following table:									
145557	Advanced Calculus of Variations (**)	6	42	MAT/05		N.A.			
145507	Advanced Topics in Analysis (*)	6	42	MAT/05	1	Gian Paolo Leonardi			
145142	Foundations of Analysis (*)	6	42	MAT/05	2	Fabio Bagagiolo			
145434	Fourier Analysis	6	42	MAT/05	2	Marco Bonacini			
145538	Geometric Analysis	9	63	MAT/05	2	Lorenzo Mazzieri			
145258	Geometric Measure Theory	6	42	MAT/05	2	Andrea Marchese			
145259	Mathematical control theory (**)	6	42	MAT/05		N.A.			
146115	Minimal surfaces	6	42	MAT/05	1	Alessandro Carlotto			
145159	Stochastic Differential Equations	6	42	MAT/06	2	Michele Coghi Luciano Tubaro			
145908	Mathematical Physics - Differential Geometry Methods	9	63	MAT/07	2	Enrico Pagani			
145907	Mathematical Physics - Quantum relativistic Theories	9	63	MAT/07	2	Valter Moretti			
146211	Optimal transport	6	42	MAT/05	1	Andrea Pinamonti Andrea Marchese			
146213	Dynamical systems (*)	6	42	MAT/05	1	Fabio Bagagiolo			

#### **FREE CHOICE COURSES**

Students, in this track are highly recommended to choose the free courses among the courses in sector MAT/05. The courses can also be taken from the Bachelor's degree, among the following: Equazioni Differenziali Ordinarie, Calcolo delle Variazioni, Analisi Funzionale, Geometria Differenziale, if the student has not taken a similar course in the Bachelor's degree. Students may use 3 of these CFU to get a C1 certificate of English or a B1 of French, German or Spanish or for the course Scientific Writing and Presentations in English, or to take an internship, according to the rules of the Regolamento.

#### **THESIS**

The course of studies is concluded with the discussion of an original thesis providing 30 CFU or with an internship/placement, which assigns 12 CFU, followed by an original thesis providing 18 CFU. Students who choose to take a 3 CFU internship among the free choice courses have to submit an original thesis worth 30 CFU

Curriculum Cryptography, Track Stage-Oriented									
Advisor o	f study: Marco Calderini								
Code	Course	CFU	Hours	SSD	Year - Sem	Lecturer			
MANDAT	ORY								
Foreign language (3CFU) – See the introduction, point 6									
CORE CO	OURSES								
145441	Algebraic Cryptography Cryptography Finite Fields and Symmetric Cryptography	6 6	42 42	MAT/02	I. 1 2	Massimiliano Sala			
145394	Coding Theory and Applications	6	42	MAT/02	1.1	Nadir Murru			
145135	Computational Algebra	6	42	MAT/02	l.1	Alessandra Bernardi			
145157	Stochastic Processes (I modulo)	6	42	MAT/06	1	Sonia Mazzucchi			
145427	Scientific Computing	9	72	MAT/08	2	Robert Nürnberg			
COMPLEMENTARY COURSES									
The follo	wing three courses:								
145508	Advanced Programming of Cryptographic Methods	6	48	INF/01	II.1	Silvio Ranise			
145937	Introduction to computer and network security	6	48	ING- INF/05	l.1	Mut DISI (0517H - cod. 145937)			
145777	Applied Cryptography	6	42	MAT/02	l.1	Marco Calderini			
At least	18 credits in the following table:								
145451	Computability and computational complexity	6	48	MAT/01	1	Mut DISI (0517H - cod. 145451)			
146117	Advanced Coding Theory	6	42	MAT/02	2	Marco Calderini			
146116	Advanced Cryptography	6	42	MAT/02	II.1	Edoardo Ballico			
145953	Advanced number theory (**)	6	42	MAT/02		N.A.			
145212	Discrete Fourier Analysis	6	42	MAT/02	2	Alessio Meneghetti			
145256	Statistics of Stochastic Processes	6	48	MAT/06	1	Claudio Agostinelli			
145396	Formal Techniques for Cryptographic Protocol Analysis	6	42	INF/01	2	Roberto Zunino			
145192	Data Hiding (**)	6	48	ING- INF/03		N.A. Mut DISI (0340H – 145614)			
145190	Digital Signal Processing	6	48	ING- INF/03	1	Mut DISI (0346H - cod. 146224)			
145056	Formal methods	12	96	ING- INF/05	2	Mut DISI (0517H - cod. 145056)			

To complement the preparation in this *track*, students who have not attended courses focused on Java programming in the Bachelor's degree are highly recommended to take the course *Laboratorio di Programmazione*. Other recommended courses from the bachelor degree program are: *Teoria Algebrica dei Numeri and Teoria di Galois* 

Students are recommended to use 3 of these CFU to get a C1 certificate of English.

#### **THESIS**

The course of studies is concluded either with the discussion of an original thesis, providing 30 CFU or with an internship/placement, which assigns 12 CFU, followed by an original thesis providing 18 CFU.

	Curriculum Cryptography, Track Research-Oriented									
Advisor o	f study: Marco Calderini									
Code	Course	CFU	Hours	SSD	Year - Sem	Lecturer				
MANDAT	TORY									
Foreign la	anguage (3CFU) – See the introduction, point 6									
CORE C	OURSES									
145441	Algebraic Cryptography Cryptography Finite Fields and Symmetric Cryptography	6 6	42 42	MAT/02	I. 1 2	Massimiliano Sala				
145394	Coding Theory and Applications	6	42	MAT/02	I.1	Nadir Murru				
145135	Computational Algebra	6	42	MAT/02	I.1	Alessandra Bernardi				
udents ca	an choose between the pair									
145256	Statistics of Stochastic Processes	6	48	MAT/06	1	Claudio Agostinelli				
145435	Stochastic Processes	9	63	MAT/06	1	Stefano Bonaccorsi				
or		· ·			•					
145157	Stochastic Processes (I modulo)	6	42	MAT/06	1	Sonia Mazzucchi				
145907	Mathematical Physics - Quantum relativistic Theories	9	63	MAT/07	2	Valter Moretti				

COMPLEMENTARY COURSES								
The following three courses:								
146116	Advanced Cryptography	6	42	MAT/02	II.1	Edoardo Ballico		
146117	Advanced Coding Theory	6	42	MAT/02	2	Marco Calderini		
145396	Formal Techniques for Cryptographic Protocol Analysis	6	42	INF/01	2	Roberto Zunino		
At least 18 credits in the following table:								
145560	Advanced Group Theory (*)	6	42	MAT/02	1	Mima Stajnokovski		
145953	Advanced Number Theory (**)	6	42	MAT/02		N.A.		
145131	Algebraic Geometry I	6	42	MAT/03	1	Edoardo Ballico Alessandro Oneto		
145777	Applied Cryptography	6	42	MAT/02	1	Marco Calderini		
145212	Discrete Fourier Analysis	6	42	MAT/02	2	Alessio Meneghetti		

Students of this *track* are **highly recommended** to choose the free courses among the courses in the sectors MAT/02-03. The courses can also be taken from the bachelor's degree; *Algebra Commutativa*, *Teoria algebrica dei numeri* and *Teoria di Galois* are particularly suggested.

Students are recommended to use 3 of these CFU to get a C1 certificate of English.

#### **THESIS**

The course of studies is concluded either with the discussion of an original thesis, providing 30 CFU or with an internship/placement, which assigns 12 CFU, followed by an original thesis providing 18 CFU.

Advisor o	f study: Veronica Vinciotti					
Code	Course	CFU	Hours	SSD	Year - Sem	Lecturer
MANDAT	ORY					
Foreign la	anguage (3CFU) – See the introduction	on, point 6	3			
CORE C	OURSES					
145905	Geometry and Topology for Data Analysis	6	42	MAT/03	1.2	Alessandro Oneto
145145	Mathematical Biology	9	72	MAT/05	l.1	Simone Pezzuto
145435	Stochastic Processes	9	63	MAT/06	l.1	Stefano Bonaccorsi
145427	Scientific Computing	9	72	MAT/08	1.2	Robert Nürnberg
145256	Statistics of stochastic processes	6	48	MAT/06	II.1	Claudio Agostinelli
COMPLE	MENTARY COURSES					
145909	Tensor Decomposition for Big Data Analysis	6	42	MAT/02	l.1	Alessandra Bernardi
145434	Fourier Analysis	6	42	MAT/05	II.2	Marco Bonacini
145902	Advanced Statistical Methods	6	42	MAT/06	1.2	Claudio Agostinelli
145561	Bayesian Statistics	6	42	MAT/06	1.2	Pier Luigi Novi Inverardi Claudio Agostinelli
145914	Statistical Models	6	42	MAT/06	l.1	Veronica Vinciotti
146049	Graphical Models and Network Science	6	42	MAT/06	II.1	Veronica Vinciotti
FREE CH	IOICE COURSES					
analysis o Students Scientific	or probability theory, it is possible to in may use 3 of these CFU to get a C1 Writing and Presentations in English	nclude her certificate	re appropr of English	iate cours or a B1 o	es (in Italian) to French, Ger	
145159	Stochastic Differential Equations	6	42	MAT/06	2	Luciano Tubaro
145152	Numerical Methods for PDEs	6	48	MAT/08	2	Robert Nürnberg
146213	Dynamical systems  Markov Decision Processes and	6	42	MAT/05	1	Fabio Bagagiolo Luigi Amedeo Bianchi
146214	Reinforcement Learning	6	48	MAT/06	1	Francesco Giuseppe Cordoni
146211	Optimal transport	6	42	MAT/05	1	Andrea Pinamonti Andrea Marchese
145903	Deep Learning	6	48	INF/01	2	Mut DISI (0342H - cod.145857 Machin Learning (mod. II))
145062	Machine Learning	6	48	INF/01	1	Mut DISI (0517H - cod. 145062)
145855	Actuarial Mathematics for Life Insurance	6	42	MAT/06	2	Daniela Yordanova Tabakova
THESIS						

#### Curriculum Mathematics and Statistics for Life and Social Sciences, Track Modelling, Statistics and Analysis of Biosystems Advisor of study: Andrea Pugliese Code Course **CFU** Hours SSD Year - Sem Lecturer **MANDATORY** Foreign language (3CFU) - See the introduction, point 6 **CORE COURSES** The following five courses 145145 | Mathematical Biology 9 72 MAT/05 1.1 Simone Pezzuto Alberto Valli (condivide 6 CFU con l'a.d. 42 MAT/05 1 145139 Partial Differential Equations 6 145393 I mod) 145256 Statistics of Stochastic Processes 6 MAT/06 II.1 Claudio Agostinelli 48 145435 Stochastic Processes 9 63 MAT/06 1.1 Stefano Bonaccorsi 145427 Scientific Computing 9 72 MAT/08 1.2 Robert Nürnberg **COMPLEMENTARY COURSES** The following five courses Simone Pezzuto 145133 Advanced Topics in Biomathematics MAT/05 1.2 6 48 Cinzia Soresina 145914 | Statistical Models 42 MAT/06 1.1 6 Veronica Vinciotti Mut. QCB (0521H - mod. Molecular 145588 Molecular Biology of the Cell 6 48 **BIO/10** 1.1 basis of Cell Structure and Function cod. 145550) INF/01 145136 Data Analysis and Exploration 48 6 1.2 Mario Lauria Mut QCB (0521H - mod. Network 145910 **Network Modeling and Simulation** 6 48 INF/01 1.1 Modeling and Simulation - cod. 146089) At least one of the following: MAT/05 1.2 145434 Fourier Analysis 6 42 Marco Bonacini 145902 **Advanced Statistical Methods** MAT/06 Claudio Agostinelli 6 42 1.2 Pierluigi Novi Inverardi **Bayesian Statistics** 42 MAT/06 1.2 145561 6 Claudio Agostinelli Michele Coghi MAT/06 145159 Stochastic Differential Equations 6 42 1.2 Luciano Tubaro Biomedical Applications of Lucas Omar Müller 145429 3 21 MAT/08 1.2 Mathematics Mathematical Aspects of 145331 6 42 MAT/08 II.1 Ana María Alonso Rodríguez Bioelectromagnetism and Imaging Numerical Methods for PDEs 6 48 MAT/08 1.2 145152 Robert Nürnberg 146213 Dynamical systems (\*) 6 42 MAT/05 1 Fabio Bagagiolo 145259 Mathematical control theory (\*\* 42 MAT/05 N.A. 6 Markov Decision Processes and Luigi Amedeo Bianchi 146214 6 48 MAT/06 1 Reinforcement Learning Francesco Giuseppe Cordoni **Graphical Models and Network** 146049 6 MAT/06 II.1 Veronica Vinciotti 42 Science Mut. DISI (0342H - cod.145857 Machine 145903 Deep Learning 6 48 INF/01 2 Learning (mod. II)) INF/01 145062 Machine Learning 6 48 1 Mut. DISI (0517H - cod. 145062) ING-Mut. QCB (0521H - cod. 145547 Mod. 145053 6 48 Laboratory of Biological Data Mining 1 INF/05 Laboratory of Biological Data Mining) **FREE CHOICE COURSES**

Free courses are suggested to be chosen from the list above.

For students missing some prerequisites in mathematical analysis or probability theory, it is possible to include here appropriate courses (in Italian) from the Bachelor's degree.

Students may use 3 of these CFU to get a C1 certificate of English or a B1 of French, German or Spanish or for the course Scientific Writing and Presentations in English.

#### **THESIS**

The course of studies is concluded either with the discussion of an original thesis, providing 30 CFU or with an internship/placement, which assigns 12 CFU, followed by an original thesis providing 18 CFU.

#### Curriculum Mathematics and Statistics for Life and Social Sciences, *Track Modelling and Simulation for Biomedical Applications*

	Advisor of	f study:	Lucas	Omar	Müller
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71071001 0	- otaay. Eacac Omar Manor					
Code	Course	CFU	Hours	SSD	Year - Sem	Lecturer
MANDAT	TORY					
Foreign la	anguage (3CFU) – See the introduction,	point 5				
CORE C	OURSES					
145145	Mathematical Biology	9	72	MAT/05	l.1	Simone Pezzuto
145139	Partial Differential Equations	6	42	MAT/05	1	Alberto Valli (condivide 6 CFU con l'a.d. 145393   mod)
145331	Mathematical Aspects of Bioelectromagnetism and Imaging	6	42	MAT/08	II.1	Ana María Alonso Rodríguez
145152	Numerical Methods for PDEs	6	48	MAT/08	1.2	Robert Nürnberg
145427	Scientific Computing	9	72	MAT/08	1.2	Robert Nürnberg
COMPLE	MENTARY COURSES					
The follo	owing five courses					
145434	Fourier Analysis	6	42	MAT/05	1.2	Marco Bonacini
145428	Computational Haemodynamics	9	72	MAT/08	II.1	Lucas Omar Müller
145338	Bio-Medical Imaging	6	48	FIS/07	1.2	Mut. FIS (0518H - cod. 145338
145332	Theoretical biomechanics (I modulo) Theoretical biomechanics (II modulo)	6 3	46 26	ICAR/01	l. 1 l. 2	Davide Bigoni Luigi Fraccarollo
145392	Physiological flow and transport in porous tissues	6	42	ICAR/02	II.1	Alberto Bellin
At least	6 CFU among the following courses:					
145914	Statistical Models	6	42	MAT/06	I.1	Veronica Vinciotti
145429	Biomedical Applications of Mathematics	3	21	MAT/08	1.2	Lucas Omar Müller
145133	Advanced Topics in Biomathematics	6	48	MAT/05	1.2	Simone Pezzuto Cinzia Soresina
145159	Stochastic Differential Equations	6	42	MAT/06	1.2	Michele Coghi Luciano Tubaro
145235	Molecular and Cellular Biophysics	6	48	BIO/10	l.1	Mut.FIS (0518H - cod. 145235)
FREE CH	HOICE COURSES					
For stud courses ( Students	are suggested to take the free courses a ents missing some prerequisites in math in Italian) from the Bachelor's degree. may use 3 of these CFU to get a C1 cert Writing and Presentations in English	nematica	ıl analysis	or probabili	ty theory, it is po	ssible to include here appropriate
145259	Mathematical Control Theory (**)	6	42	MAT/05		N.A.
145561	Bayesian Statistics	6	42	MAT/06	1.2	Pierluigi Novi Inverardi

	<u> </u>					
145259	Mathematical Control Theory (**)	6	42	MAT/05		N.A.
145561	Bayesian Statistics	6	42	MAT/06	1.2	Pierluigi Novi Inverardi Claudio Agostinelli
146049	Graphical Models and Network Science	6	42	MAT/06	II.1	Veronica Vinciotti
146213	Dynamical systems	6	42	MAT/05	1	Fabio Bagagiolo
146214	Markov Decision Processes and Reinforcement Learning	6	48	MAT/06	1	Luigi Amedeo Bianchi Francesco Giuseppe Cordoni
145062	Machine Learning	6	48	INF/01	1	Mut DISI (0517H - cod. 145062)
145855	Actuarial Mathematics for Life Insurance	6	42	MAT/06	2	Daniela Yordanova Tabakova

#### **THESIS**

The course of studies is concluded either with the discussion of an original thesis, providing 30 CFU or with an internship/placement, which assigns 12 CFU, followed by an original thesis providing 18 CFU.

	Curriculum Mathematics Track Modelling, Statist					
Advisor o	f study: Stefano Bonaccorsi		<u></u>			
Code	Course	CFU	Hours	SSD	Year - Sem	Lecturer
MANDAT	ORY					
Foreign la	anguage (3CFU) – See the introduction, point	t 6				
CORE CO	DURSES					
145139	Partial Differential Equations	6	42	MAT/05	1	Alberto Valli (condivide 6 CFU con l'a.d. 145393 ı mod
145145	Mathematical Biology	9	72	MAT/05	l.1	Simone Pezzuto
145256	Statistics of Stochastic Processes	6	48	MAT/06	II.1	Claudio Agostinelli
145435	Stochastic Processes	9	63	MAT/06	l.1	Stefano Bonaccorsi
At least	one of the following					
145152	Numerical Methods for PDEs	6	48	MAT/08	1.2	Robert Nürnberg
145427	Scientific Computing	9	72	MAT/08	1.2	Robert Nürnberg
COMPLE	MENTARY COURSES – At least 39 CFU					
145914	Statistical Models	6	42	MAT/06	l.1	Veronica Vinciotti
145159	Stochastic Differential Equations	6	42	MAT/06	1.2	Michele Coghi Luciano Tubaro
The rema	aining CFU among the following					
145905	Geometry and Topology for Data Analysis	6	42	MAT/03	1.2	Alessandro Oneto
145902	Advanced Statistical Methods	6	42	MAT/06	1.2	Claudio Agostinelli
145561	Bayesian Statistics	6	42	MAT/06	1.2	Pier Luigi Novi Inverardi Claudio Agostinelli
146213	Dynamical systems	6	42	MAT/05	1	Fabio Bagagiolo
146214	Markov Decision Processes and Reinforcement Learning	6	48	MAT/06	1	Luigi Amedeo Bianchi Francesco Giuseppe Cordoni
145912	Scientific Programming	6	48	INF/01	1	Mut QCB (0521H Scientific programming – mod. Programming – cod. 145540)
121395	Financial markets and economic activity	6	36	SECS-P/01	1	Mut DEM (0119H – cod. 121395)
121469	Mercati e Intermediari Finanziari Progredito	10	60	SECS-P/11	2	Mut DEM (0122H – cod. 121469)
121470	Strumenti di Investimento e Derivati	10	60	SECS-P/11	1	Mut DEM (0122H – cod. 121470)
121414	Workshop on Financial simulation	6	36	SECS-S/03	1	Mut DEM (0122H – cod. 121414)
145855	Actuarial Mathematics for Life Insurance	6	42	MAT/06	2	Daniela Yordanova Tabakova

Curriculum Mathematics and Statistics for Life and Social Sciences

#### **FREE CHOICE COURSES**

Students are suggested to take the free courses among those listed above and not already chosen. For students missing some prerequisites in mathematical analysis or probability theory, it is possible to include here appropriate courses (in Italian) from the Bachelor's degree.

Students may use 3 of these CFU to get a C1 certificate of English or a B1 of French, German or Spanish or for the course Scientific Writing and Presentations in English.

#### **THESIS**

The course of studies is concluded either with the discussion of an original thesis, providing 30 CFU or with an internship/placement, which assigns 12 CFU, followed by an original thesis providing 18 CFU.

Advisor o	of study: Luigi Amedeo Bianchi					
Code	Course	CFU	Hours	SSD	Sem	Lecturer
MANDAT	TORY					
Foreign la	anguage (3CFU) – See the introduction, point 6					
145151	Mathematical models for the Physical, Natural and Social Sciences (Core course)	6	42	MAT/06	1	Luigi Amedeo Bianchi
145155	Modern Physics (Complementary course)	12	84	FIS/08	1+2	Giovanni Andrea Prodi
OTHER (	CORE COURSES - At least 30 credits					
145146	Mathematical Logic	6	42	MAT/01	1	Stefano Baratella
145135	Computational Algebra	6	42	MAT/02	1	Alessandra Bernardi
145253	Foundations of Geometry	6	42	MAT/03	2	Gianluca Occhetta
145904	Elementary Mathematics from a Higher Viewpoint	6	42	MAT/04	1	Elisa Postinghel
145144	Laboratory of Didactics of Mathematics (*)	6	42	MAT/04	2	Aaron Gaio
145154	Experimental Mathematics Laboratory at School Level	6	42	MAT/04	2	Silvano Delladio
145142	Foundations of Analysis (*)	6	42	MAT/05	2	Fabio Bagagiolo
COMPLE	EMENTARY COURSES – At least one of the two	course	s			
145153	Experimental Physics Laboratory at High School Level I	6	56	FIS/08	1	Pasquale Onorato
145215	Experimental Physics Laboratory at High School Level II (*)	6	56	FIS/08	2	Pasquale Onorato
	COMPLEMENTARY COURSES - At least 12 cred	its cho	sen in the	following	table	or among the courses not
	From the previous tables  Elementary Mathematics from a Higher					
145150	Viewpoint 2	6	42	MAT/04	2	Marco Andreatta
145906	Laboratory Techniques for Mathematics Teaching	6	56	MAT/04	1	Elisabetta Ossanna
145913	Topics in History of Mathematics	6	42	MAT/04	2	Claudio Fontanari
145914	Statistical Models	6	42	MAT/06	1	Veronica Vinciotti
145820	Laboratory of Computer Science Education	6	48	INF/01		N.A. a.a. 2023/2024

#### OTHER COMPLEMENTARY COURSES - At most 6 credits

Students can choose courses in the sectors MAT/\*, FIS/\*, INF/01 offered by Master's Degrees of the University of Trento or by Master's Degree in Mathematics of the University of Verona or in the sectors M-PED/, M-PSI/1-4, M-FIL/02,05 offered by University of Trento

#### **FREE CHOICE COURSES**

Students may use 3 of these CFU to get a C1 certificate of English or a B1 of French, German or Spanish or for the course Scientific Writing and Presentations in English, or to take an internship, according to the rules of the Regolamento.

#### **THESIS**

The course of studies is concluded either with the discussion of an original thesis, providing 30 CFU or with an internship/placement, which assigns 12 CFU, followed by an original thesis providing 18 CFU. Students who choose to take a 3 CFU internship among the free choice courses have to submit an original thesis worth 30 CFU.

The courses marked with (\*) will be offered in the academic year 2023/2024 but may not be offered in the academic year 2024/2025.

#### Appendix - Glossary

Credit = Credito formativo universitario = CFU

This is the European unit for measuring the value of activities such a course, an internship, or a thesis. One credit corresponds to about 7 hours of frontal lectures, and a total of 25 hours of work for the student. 120 CFU are required for a Master.

Sector = Settore scientifico-disciplinare = SSD
 This is a nation-wide classification of University courses, sorted out in various categories. The categories (SSD) for Mathematics are the following:

	SSD	Italiano	Inglese
•	MAT/01	Logica Matematica	Mathematical Logic
•	MAT/02	Algebra	Algebra
•	MAT/03	Geometria	Geometry
•	MAT/04	Matematiche complementari	Miscellanea
•	MAT/05	Analisi matematica	Mathematical Analysis
•	MAT/06	Probabilità e	Probability and
		statistica matematica	Mathematical Statistics
•	MAT/07	Fisica matematica	Mathematical Physics
•	MAT/08	Analisi numerica	Numerical Analysis
•	MAT/09	Ricerca operativa	Operations Research

For other sectors see http://www.miur.it/UserFiles/115.htm

#### • Curriculum (pl. curricula)

Within the general framework of the Master of Science in Mathematics, it is possible to aim at gaining an in-depth knowledge and understanding of several areas of advanced Mathematics (curriculum Advanced Mathematics) or to aim more at acquiring knowledge useful for teaching and communicating mathematics and other sciences (curriculum Teaching and Scientific Communication) or to specialize in one of the curricula of Mathematics and Statistics for Life and Social Sciences or in Cryptography. Each curriculum will have different rules in the choice of courses.

#### • Study plan (Piano di studi)

Each student of the Master of Science in Mathematics has to specify the choices he is taking among the various courses in a document with this name. They have to include a certain number, for each group of Sectors, of CFU in "caratterizzanti" (= Core) courses, and in "affini" (= Complementary) courses.

#### Track = suggested study plan

Examples of possible study plans centered on different aspects of mathematical studies.

• Stage: the Italian term (actually borrowed from French) for an internship.

#### • Semester (shortened in sem.)

Teaching is arranged in two periods, conventionally called semesters = six months, although they last only about 14 weeks each. The first semester starts in mid-September and ends just before Christmas. The second semester lasts from mid-February to the end of May/beginning of June.

#### Corso mutuato = Mut

This is a course which is offered by a different Department or is a proxy for a course held in a different Department.

#### • N.A. = Not Available

A course that has been active in previous years, and may well be active again in the future, but is not currently offered.